Longitudinal Feedback Using a Low-pass Differentiator

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I.FAST Workshop 2024 on Bunch-by-Bunch Feedback Systems



Motivation

Concept

Surprise Discover

Some Observations

Future Directions

Outline

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Observations

Cummaru

- Traditionally, longitudinal feedback controllers are designed to satisfy three requirements:
 - ▶ 90° phase shift at the synchrotron frequency;
 - DC rejection;
 - Bandpass response.
- ► This approach is limited in its tune acceptance range;
- Many modern light sources use harmonic cavities to lengthen the bunches for the improved lifetime;
- This leads to wide range of synchrotron frequency variation versus beam current, as well as wide spread of frequencies at nominal operating current.

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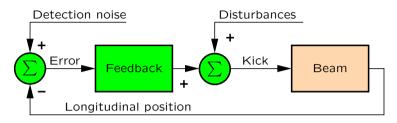
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- ▶ Beam response $B(s) = \frac{C}{s^2 2\lambda s + \omega^2}$;
- C absorbs front-end and back-end gains, as well as optics parameters;
- ▶ Differentiator F(s) = Ks is mathematically ideal to stabilize B(s):
- ► Closed loop response $H_{\rm cl}(s) = \frac{B(s)}{1+F(s)B(s)} = \frac{C}{s^2-(2\lambda-KC)s+\omega^2}$;
- ▶ Differentiator only affects the growth rate and provides constant damping independent of the synchrotron frequency.

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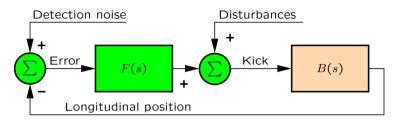
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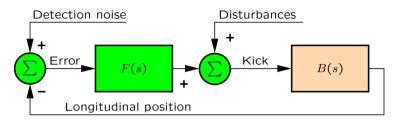
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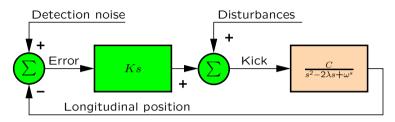
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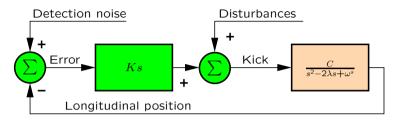
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- When I started working on longitudinal bunch-by-bunch feedback as a first year graduate student I almost immediately learned that "differentiator could never work".
- Approximate differentiator by one turn difference $u_n = z_n z_{n-1}$
- Problems
 - Very little gain at synchrotron frequencies small phase advance per turn;
 - Controller gain increases linearly with frequency output will be swamped with the amplified wideband detection and quantization noise.
- ► For me the matter rested there until summer 2022 (NAPAC 2022), when I learned that Ryan Lindberg of APS-U arrived at the differentiator idea;
- ► I set out to demonstrate why this was a bad idea and was surprised to discover that, at least in the Simulink model, it worked as well as the conventional approach;
- ► Seemed to work on the bench next step would be testing it in a machine.

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- A month later I got a call from the ALS they had trouble reaching 500 mA operating current;
- ► What is ALS:
 - 1.5 GeV storage ring with normal conducting main and harmonic RF cavities;
 - Multiple unstable modes in the longitudinal plane;
 - Zero current synchrotron frequency of 8.5 kHz decreases to 5.5 kHz at full current due to the action of the harmonic cavities;
 - Mode 0 is shifted to 4 kHz by the interaction with the main RF impedance, normally stable.
- ► Feedback filter for the ALS is designed to damp instabilities from 5 to 9 kHz, rolls off gently below 5 kHz to avoid destabilizing mode 0.
- ▶ In September 2022, mode 0 was going unstable at the ALS and the existing feedback filter could not damp the instability;
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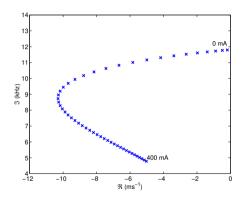
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Mode 0 vs. Beam Current



- Root locus of the modal eigenvalue versus beam current;
- Damping on the real axis, frequency on the imaginary;
- Old ALS configuration (higher RF voltage).

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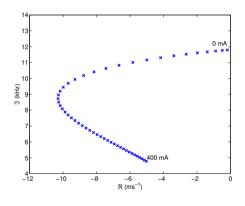
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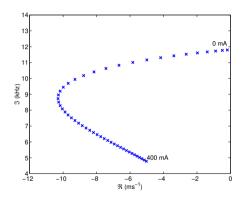
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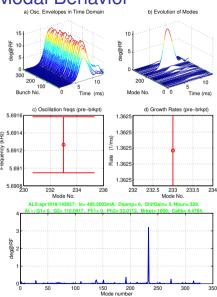
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- A grow/damp measurement from 2018:
- ▶ 12 ms growth time;
- Well-known HOMs in main RF cavities drive mode 233;
- ► A measurement on September 8 2022;
- 3 ms growth time;
- ► Modes 0, 1, and -1 grow.

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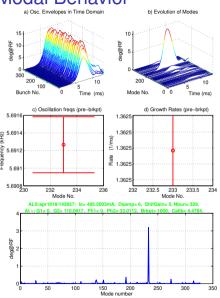
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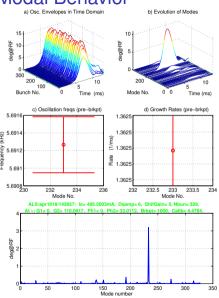
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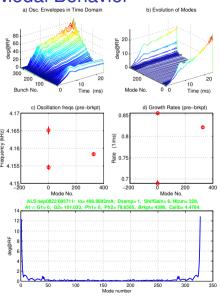
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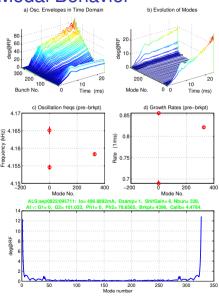
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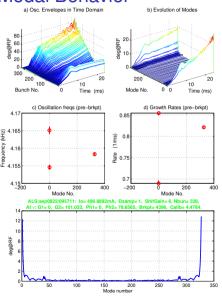
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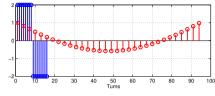
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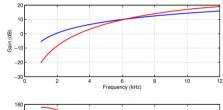
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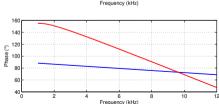
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ALS Filter Comparison







 Comparison of the normal ALS filter and a 16-tap low-pass differentiator;

- Similar gains in the working range;
- Much steeper slope for the normal filter (32 taps, downsampling of 3);
- Log scale plot over a wider frequency range.

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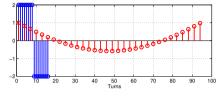
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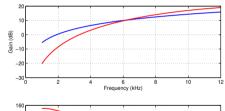
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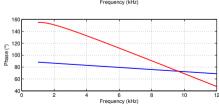
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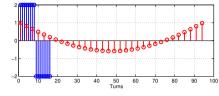
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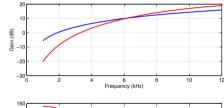
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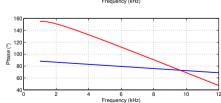
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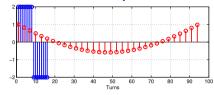
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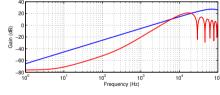
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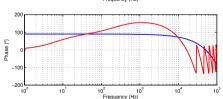
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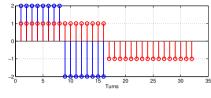
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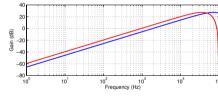
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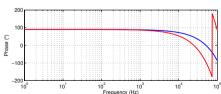
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- Since the original "emergency intervention" we have updated the ALS differentiator from 16 to 32 taps;
- Factor of 2 in the shorter filter's coefficients reflects higher shift gain
- 6 dB gain difference in the linear range;
- As expected, a longer filter has faster phase roll due to higher group delay;
- Identical peak gains.

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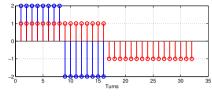
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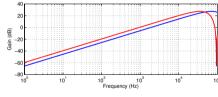
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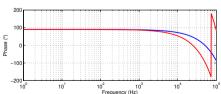
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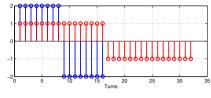
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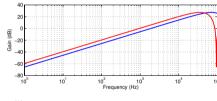
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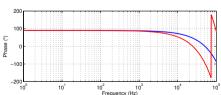
Surprise Discovery

Observations









- Since the original "emergency intervention" we have updated the ALS differentiator from 16 to 32 taps;
- Factor of 2 in the shorter filter's coefficients reflects higher shift gain;
- 6 dB gain difference in the linear range;
- As expected, a longer filter has faster phase roll due to higher group delay;
- ► Identical peak gains.

Motivation

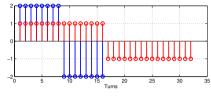
Concept

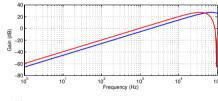
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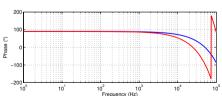
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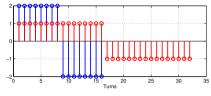
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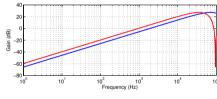
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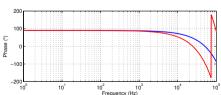
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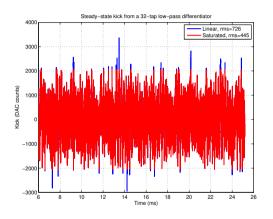
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- Standard worry differentiator will saturate the output with amplified noise, leaving no power for feedback correction;
- Steady-state kick at 500 mA with a 32-tap low-pass differentiator;
- Consistently hits full scale, reflected in the difference in the RMS kick;
- When longitudinal motion develops, power is directed exactly where it's needed.

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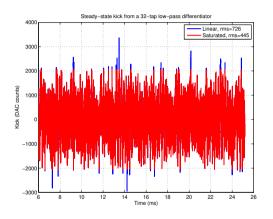
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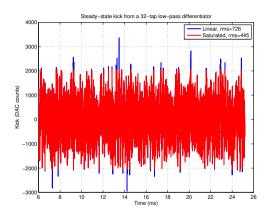
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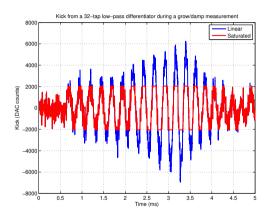
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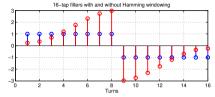
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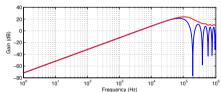
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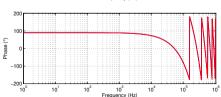
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- Boxcar low-pass differentiator is an obvious choice, but is there something better?
- Multiplied by a Hamming window
- Worse than the boxcar more high-frequency gain;
- Smooth noise-robust differentiator same problem;
- Optimization needed to maximize the ratio of in-band gain to the average high-frequency gain;
- Possibly the optimization will tell us that the boxcar is optimal...

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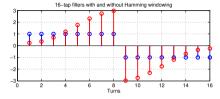
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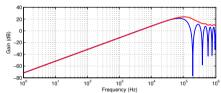
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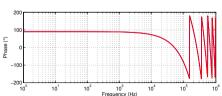
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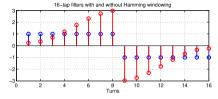
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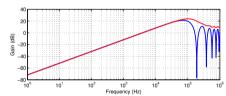
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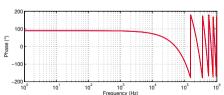
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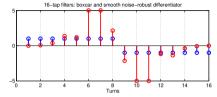
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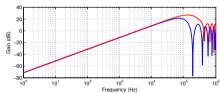
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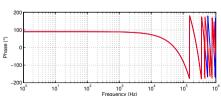
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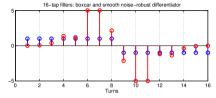
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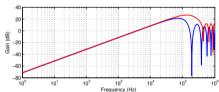
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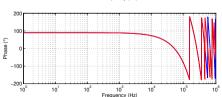
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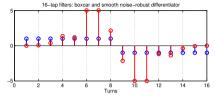
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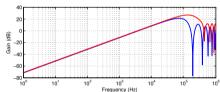
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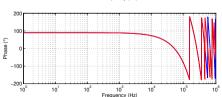
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- More research is needed to optimize the filter.
- I'd like to thank Ryan Lindberg and Michael Borland for initiating discussions of the low-pass differentiator approach!

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