

Advanced Signal Processing for APS-U

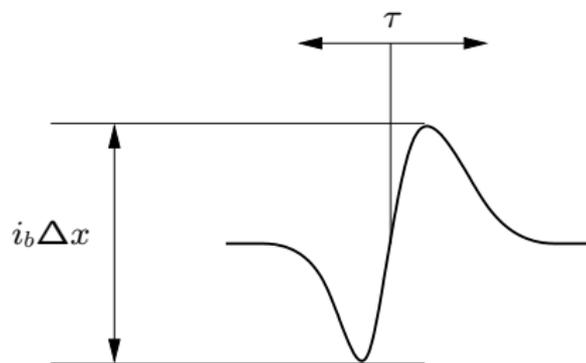
D. Teytelman

Dimtel, Inc., San Jose, CA, USA

February 16, 2018



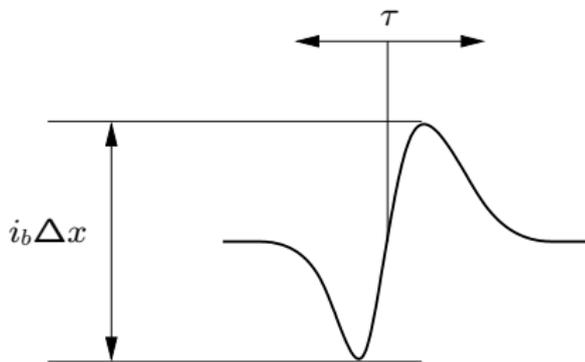
Conventional RF Front-End Signal Processing



- Horizontal difference signal derived from four buttons;
- At zero offset amplitude goes to zero;
- Replicate the pulse two or more times;
- Spaced by detection frequency period;
- For analysis can replace the complex shape with a sinusoidal burst at $M\omega_{rf}$;
- Detected signal after filtering.



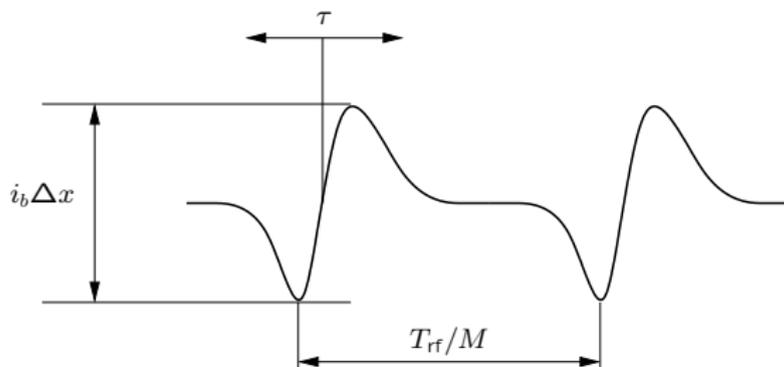
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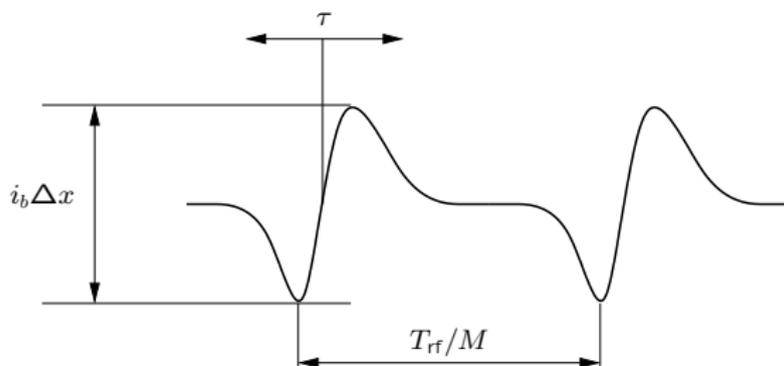
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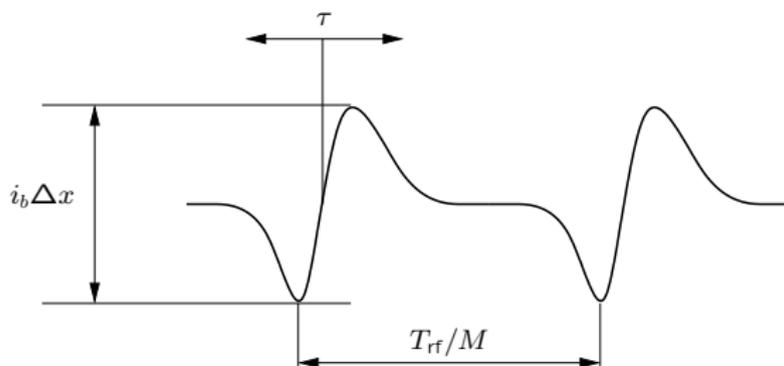
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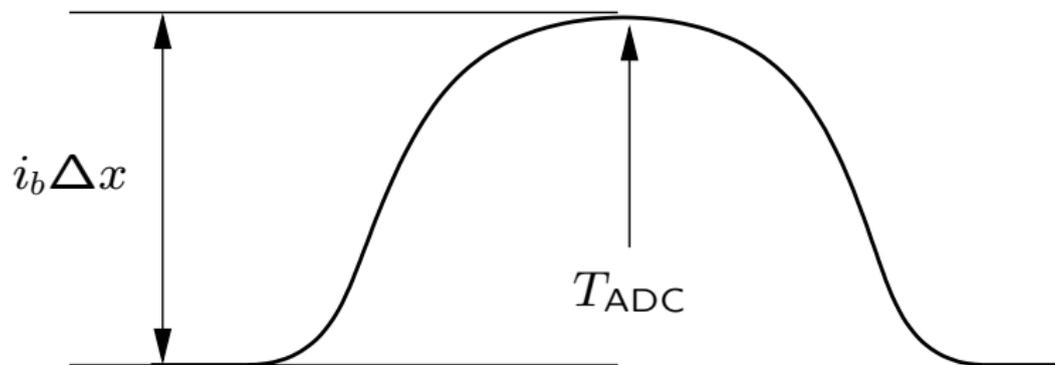
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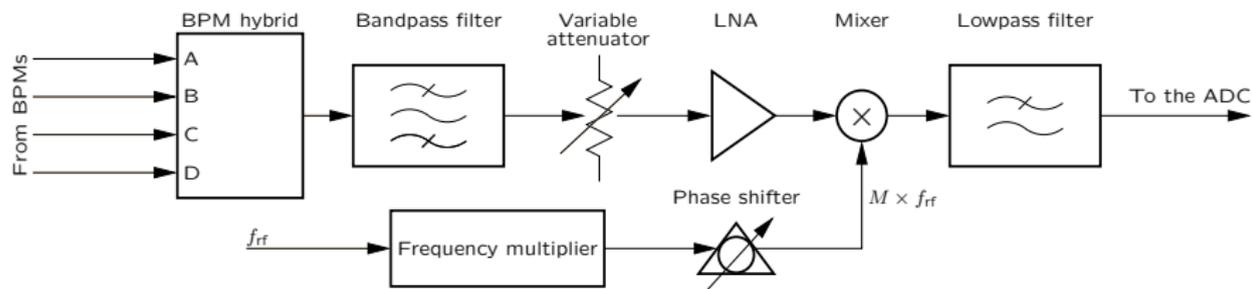
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Energy Sensing Analysis



- Conventional front-end with ΔX input;
- Model signal at detection frequency as $v(t) = A(x_0 + \Delta x) \sin(M\omega_{rf}(t + \tau))$;

Parameter	Definition
x_0	Orbit offset
Δx	Horizontal oscillation $D\epsilon/E_0$
M	Detection harmonic
τ	Time oscillation



Adding Synchrotron Oscillation

- Assume energy oscillation $\epsilon = \epsilon_0 \cos \omega_s t$;
- Dispersion term is $\Delta x = D\epsilon_0/E_0 \cos \omega_s t$;
- Time domain oscillation is $\tau = \frac{\alpha\epsilon_0}{E_0\omega_s} \sin \omega_s t$;
- Pickup gain factor $A = Q_b g_0 M$, assuming relatively low RF harmonics;
- Mixing $v(t)$ with $\cos M\omega_{rf}t$ and $\sin M\omega_{rf}t$ for phase/amplitude detection respectively;
- Amplitude signal, after low-pass filtering is $A/2(x_0 + \Delta x) \cos M\omega_{rf}\tau$;
- Further downconvert baseband output of the amplitude detector relative to synchrotron reference to extract phase shift.



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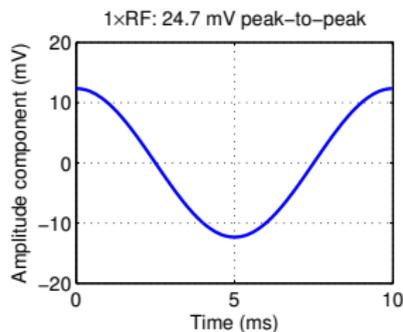
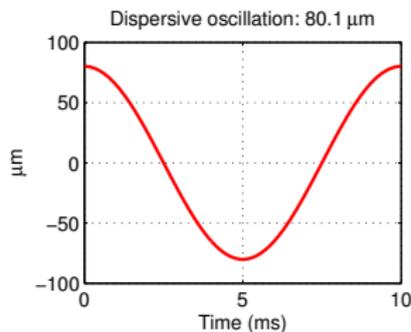
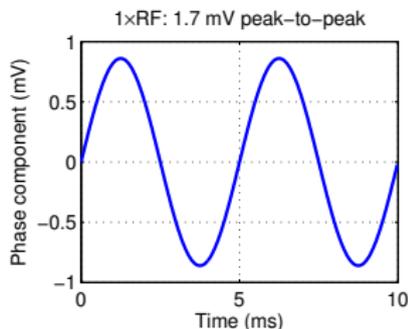
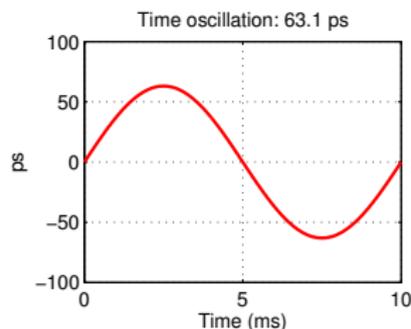


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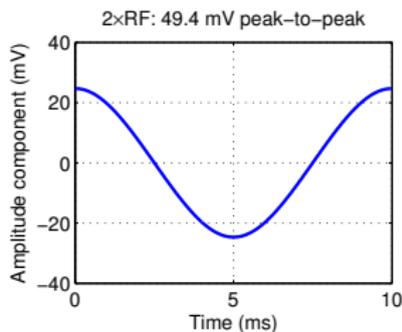
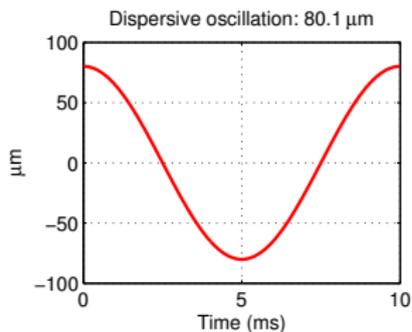
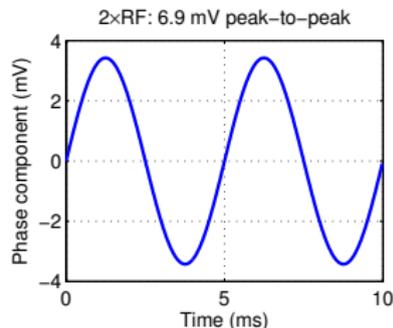
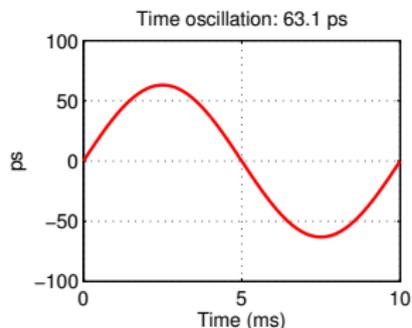
Zero Orbit Offset Case



- 352 MHz;
- 704 MHz;
- 1056 MHz;
- 1408 MHz;
- 1760 MHz;
- Linear scaling for amplitude, quadratic for phase, just as expected.



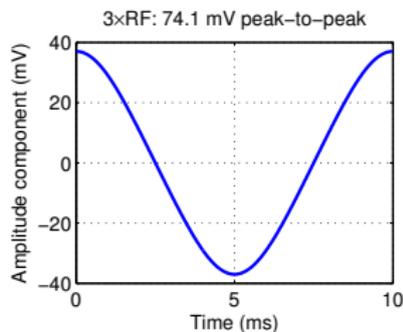
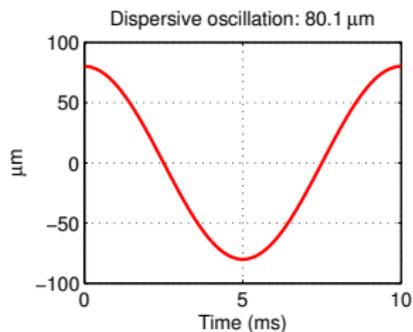
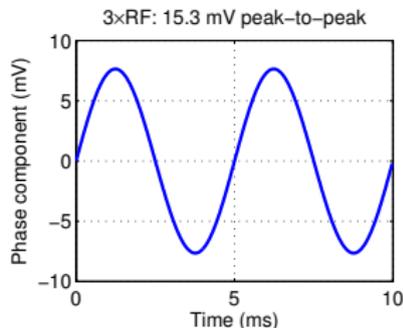
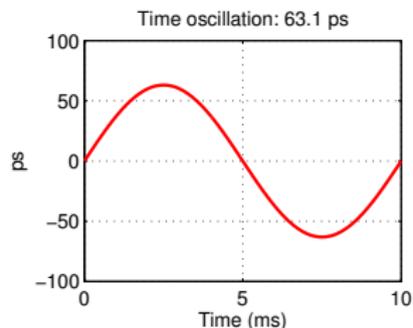
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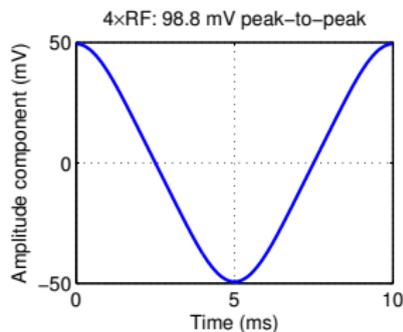
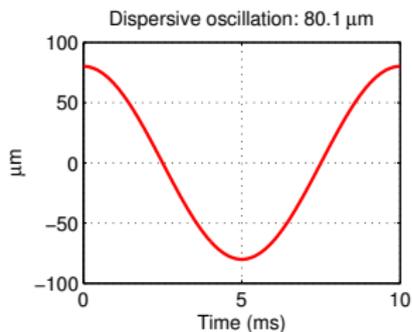
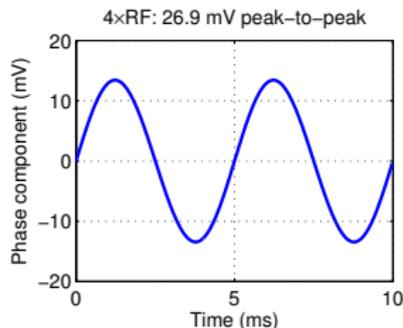
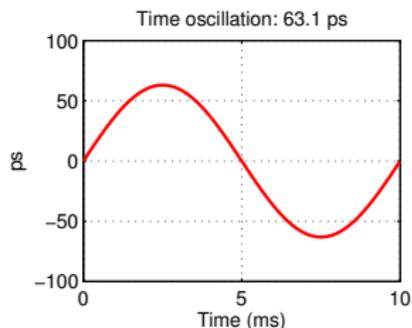
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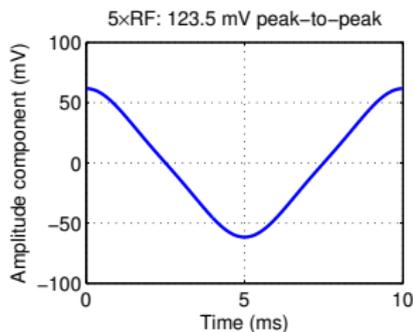
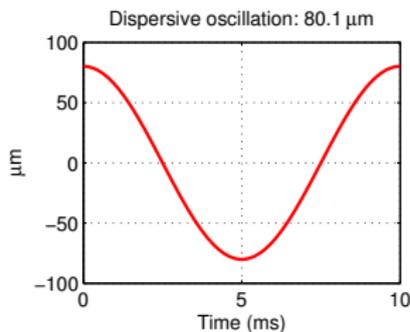
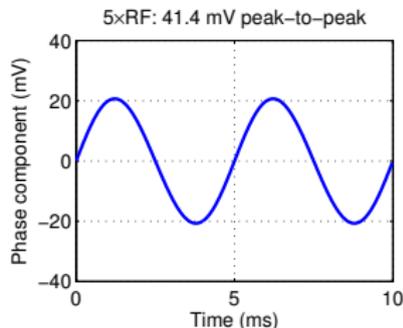
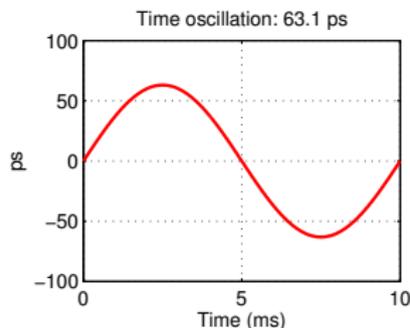
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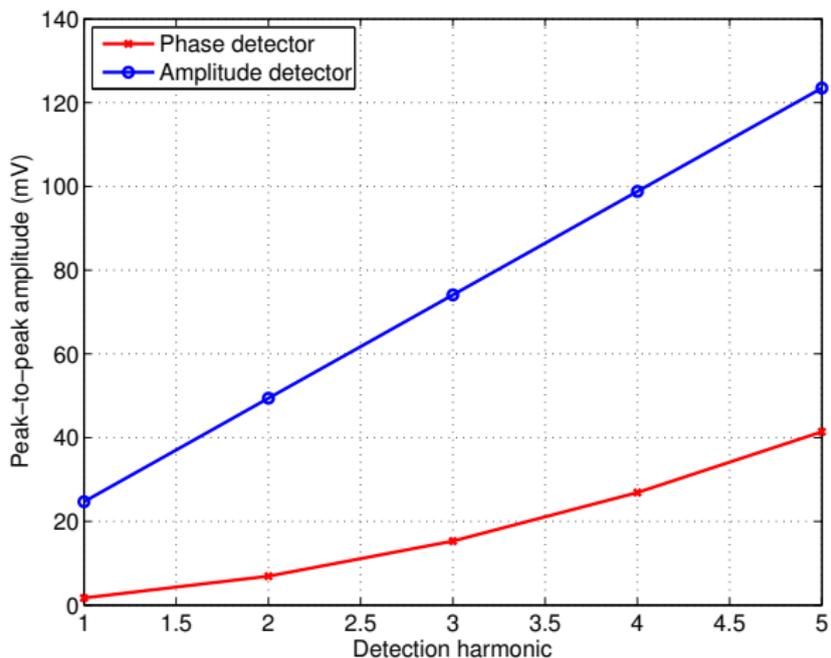
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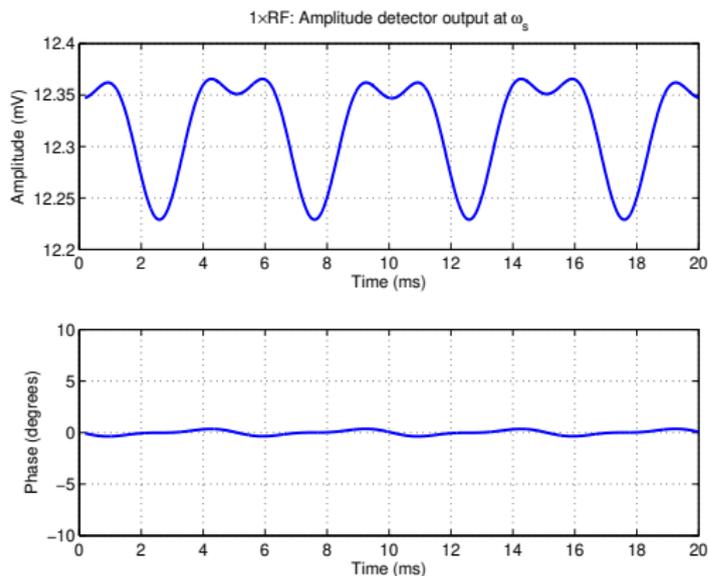
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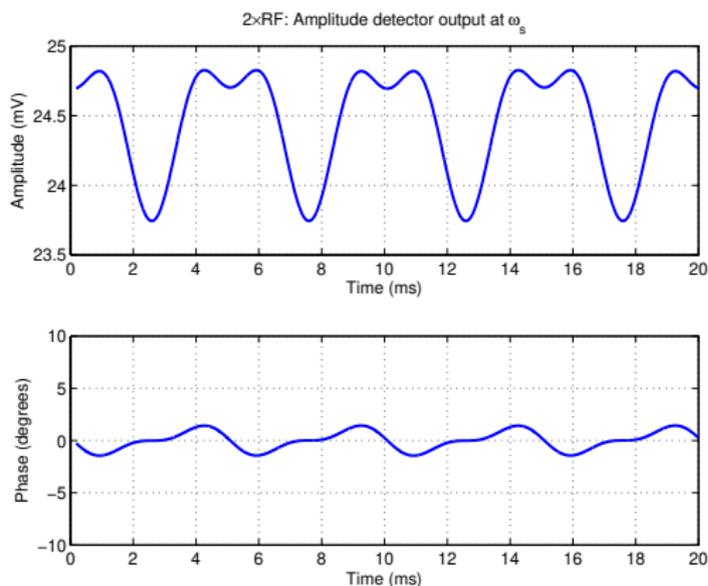
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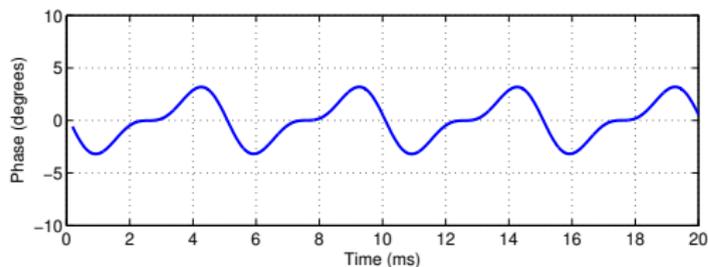
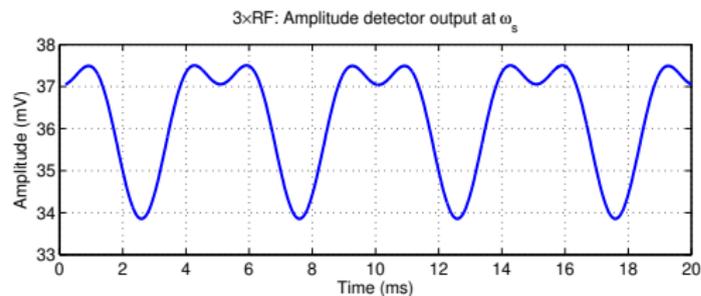
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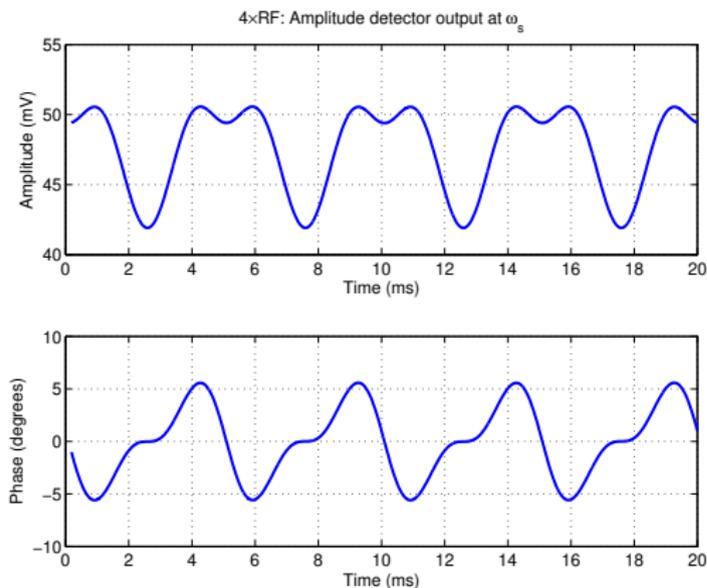
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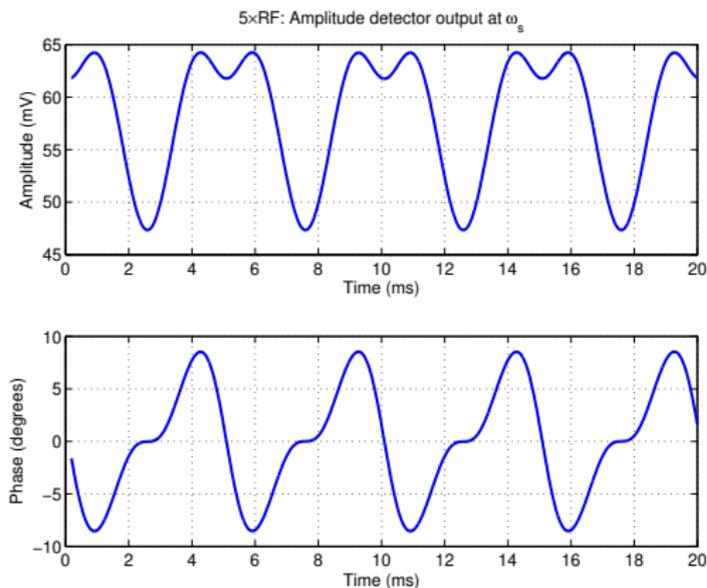
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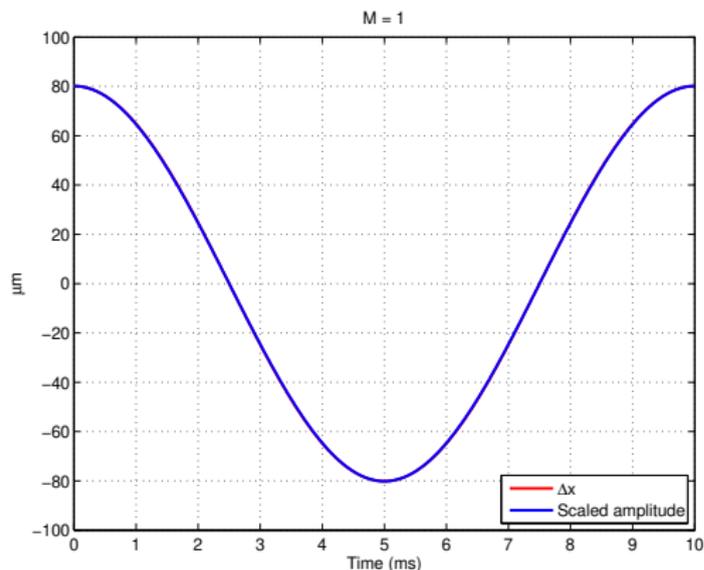
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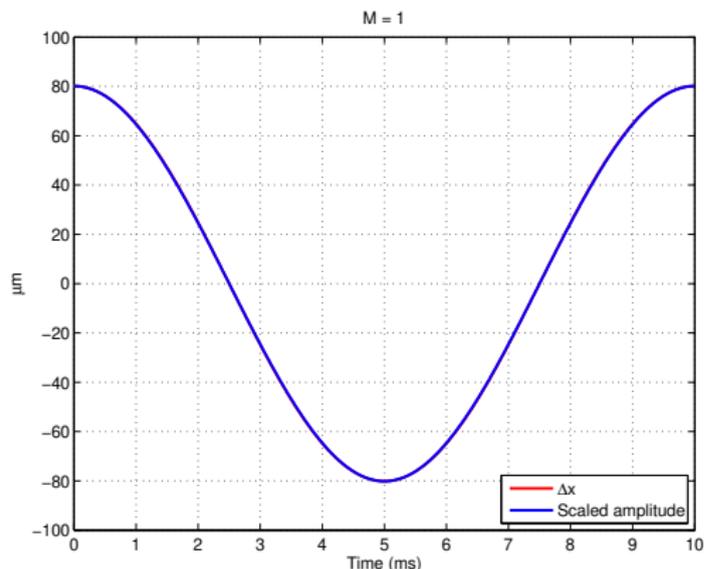
Distortion Due to Phase Modulation



- Original oscillation and detected signal;
- Nearly perfect at RF;
- Deviations from original at peak phase excursions;
- Larger effect at the third harmonic;
- And fourth;
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- Generating odd harmonics, can be harmful with wide tune spreads.



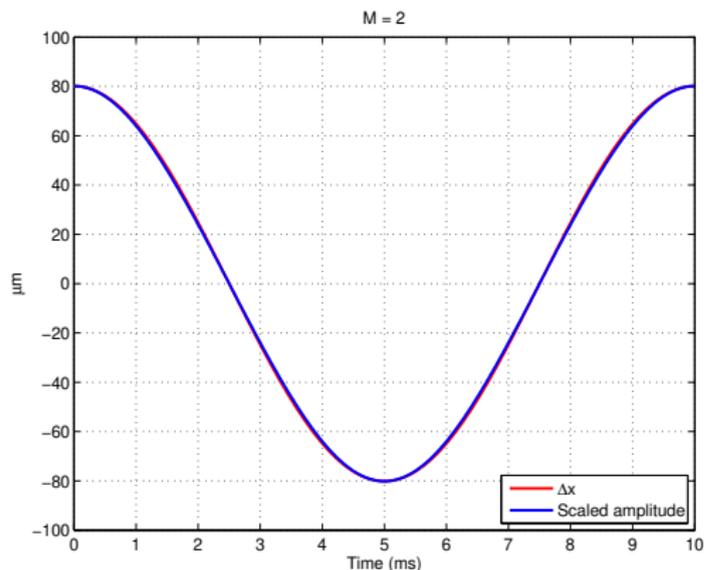
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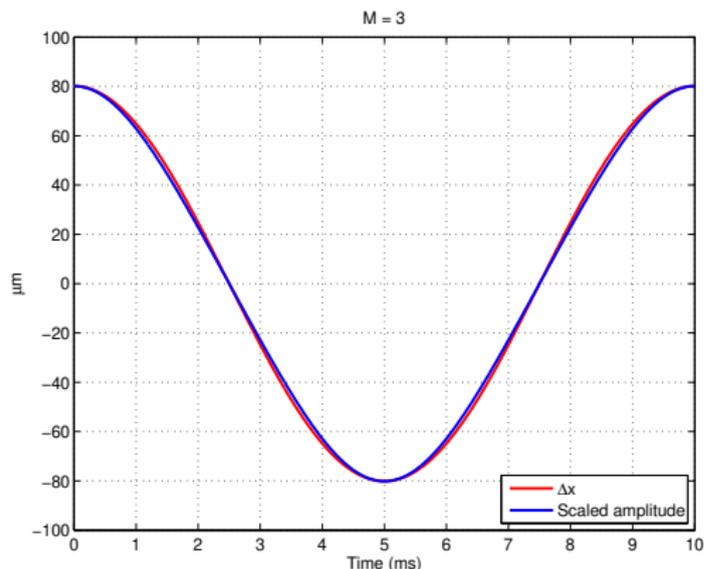
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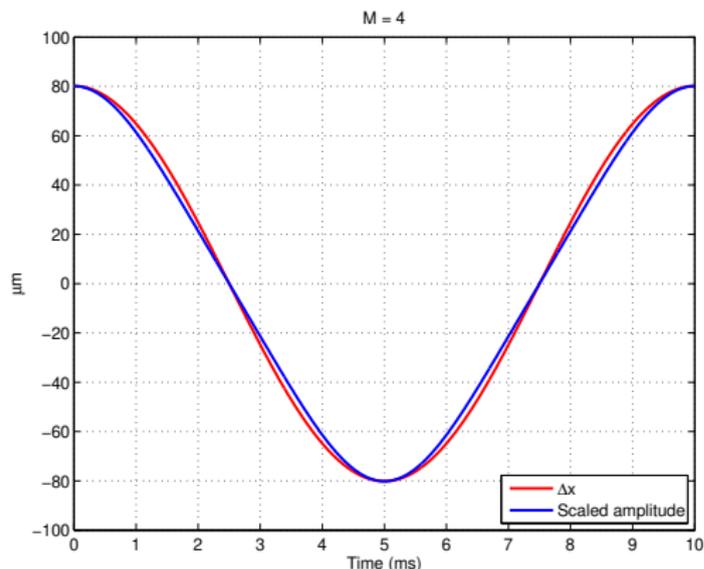
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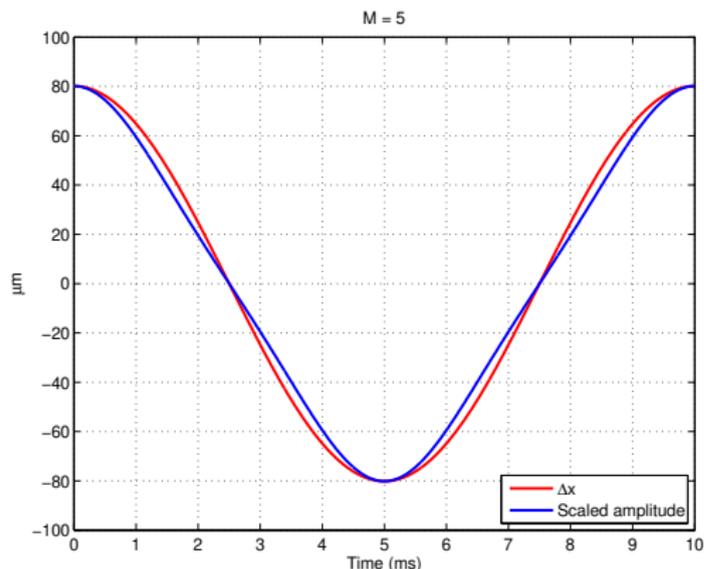
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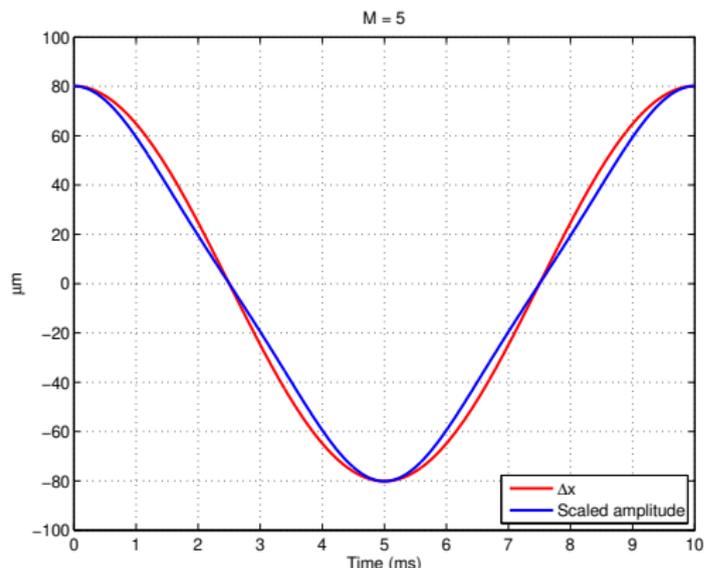
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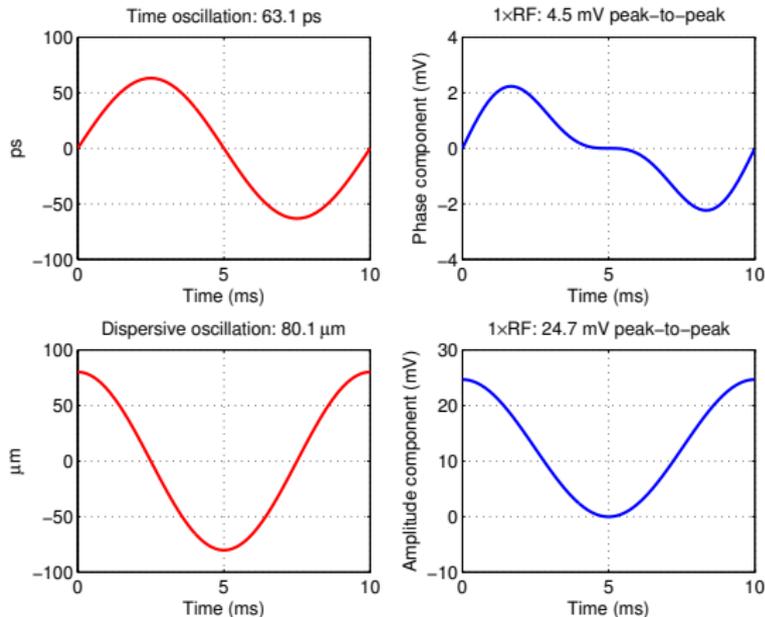
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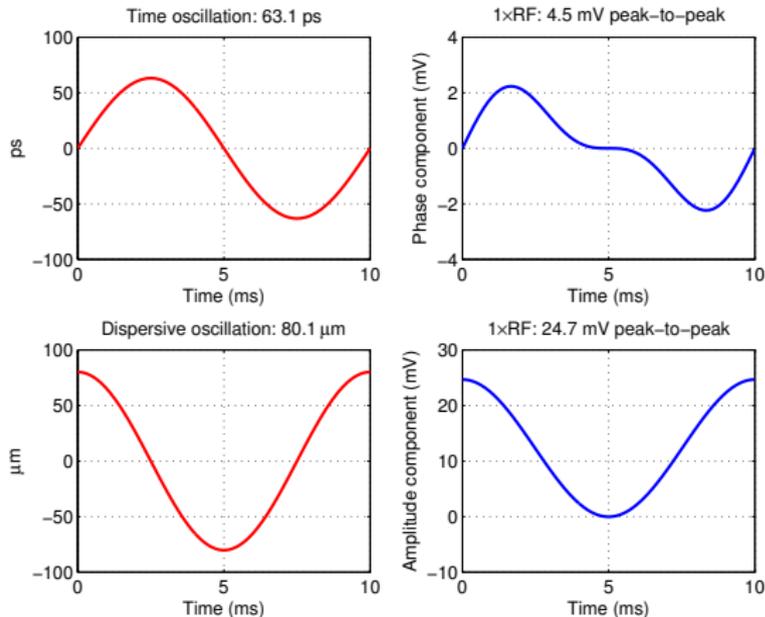
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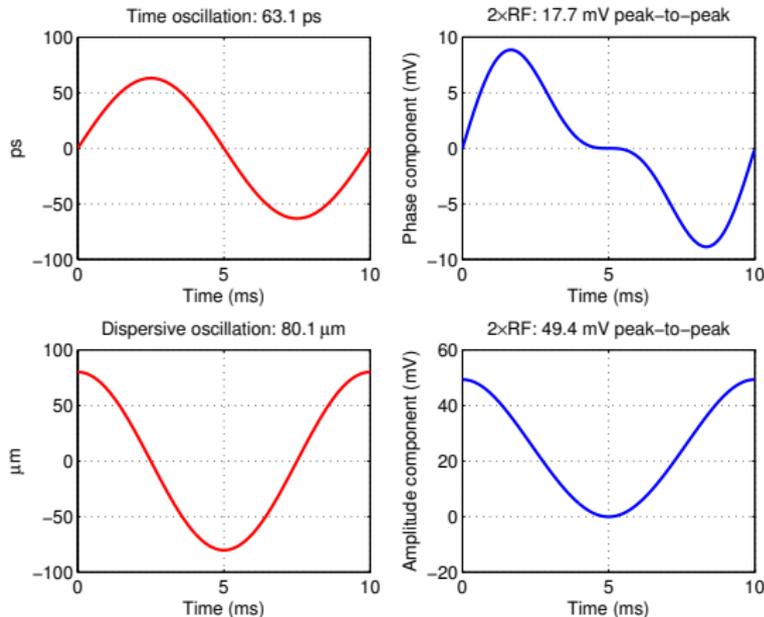
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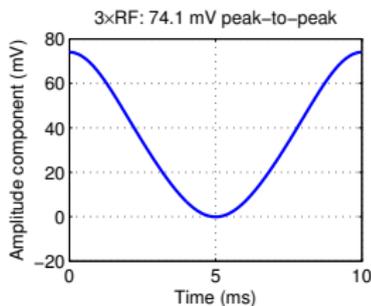
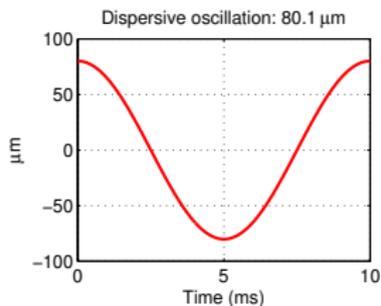
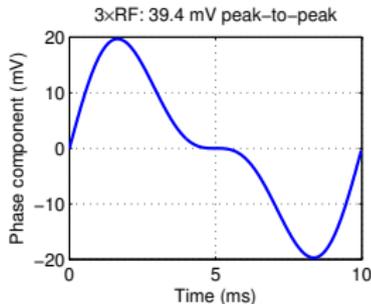
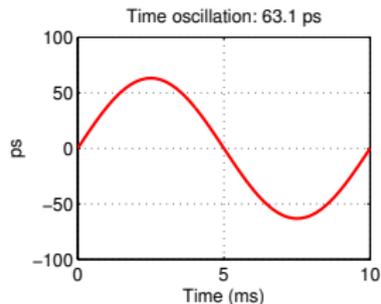
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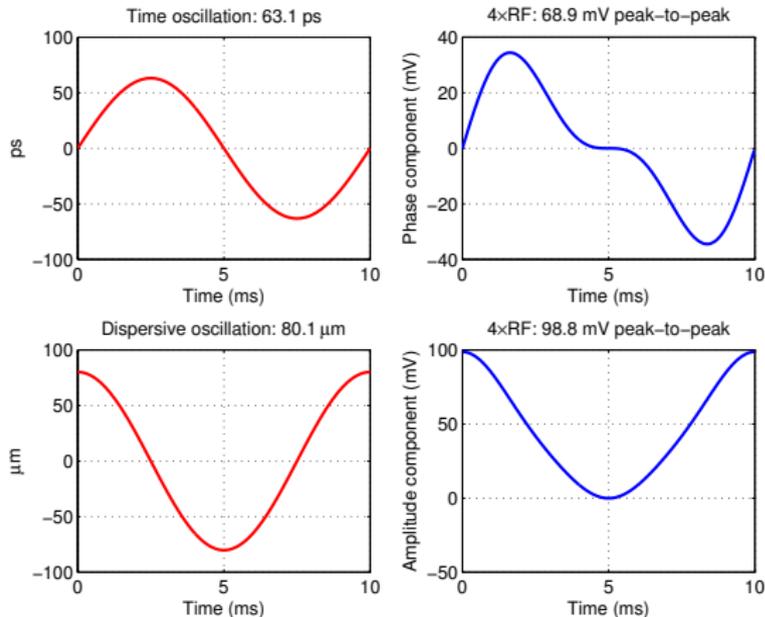
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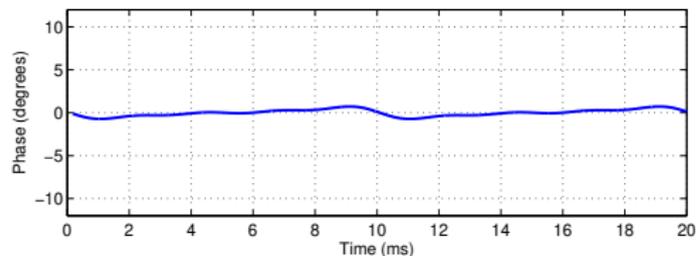
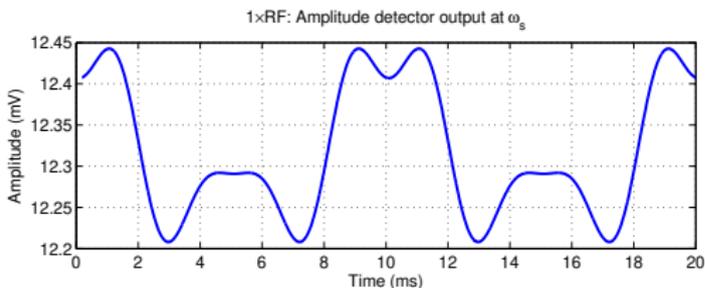
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Amplitude and Phase Relative to Synchrotron Reference, Moderate Offset Case

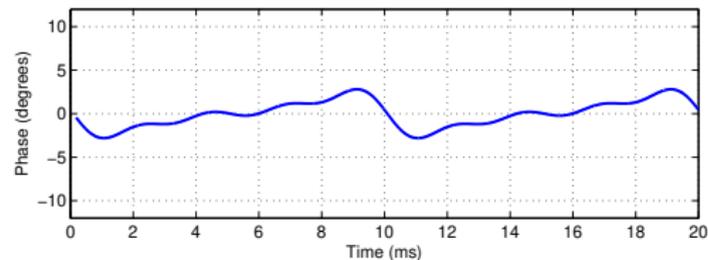
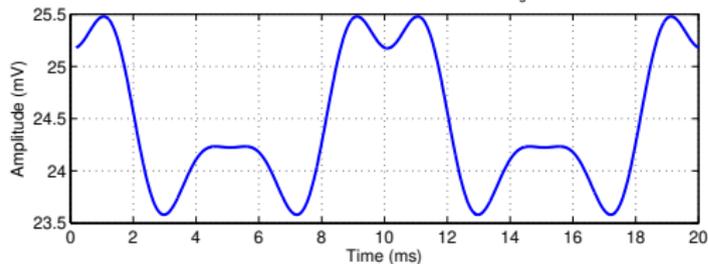


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Amplitude and Phase Relative to Synchrotron Reference, Moderate Offset Case

2xRF: Amplitude detector output at ω_s

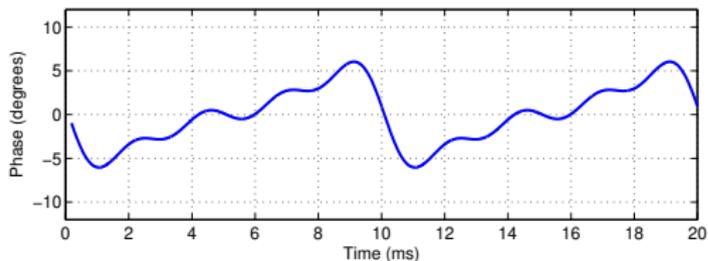
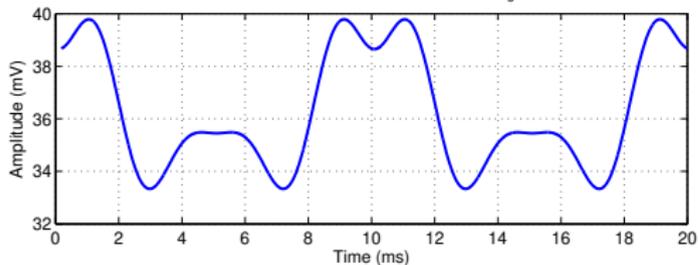


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Amplitude and Phase Relative to Synchrotron Reference, Moderate Offset Case

3×RF: Amplitude detector output at ω_s

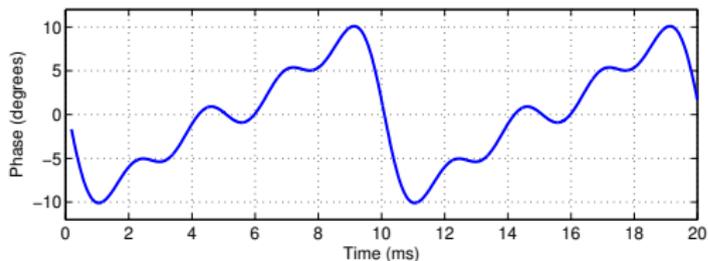
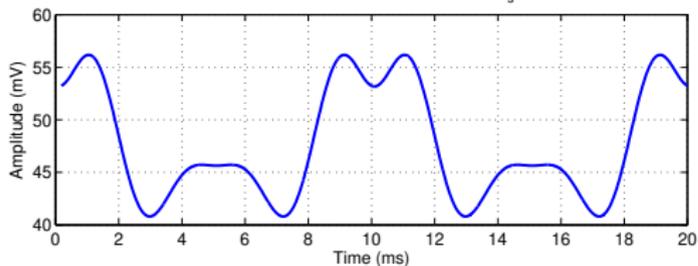


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Amplitude and Phase Relative to Synchrotron Reference, Moderate Offset Case

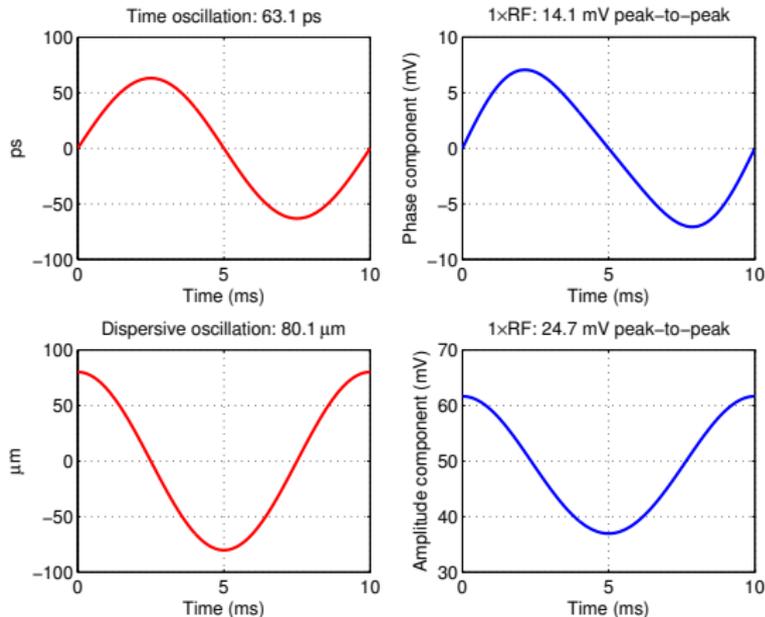
4×RF: Amplitude detector output at ω_s



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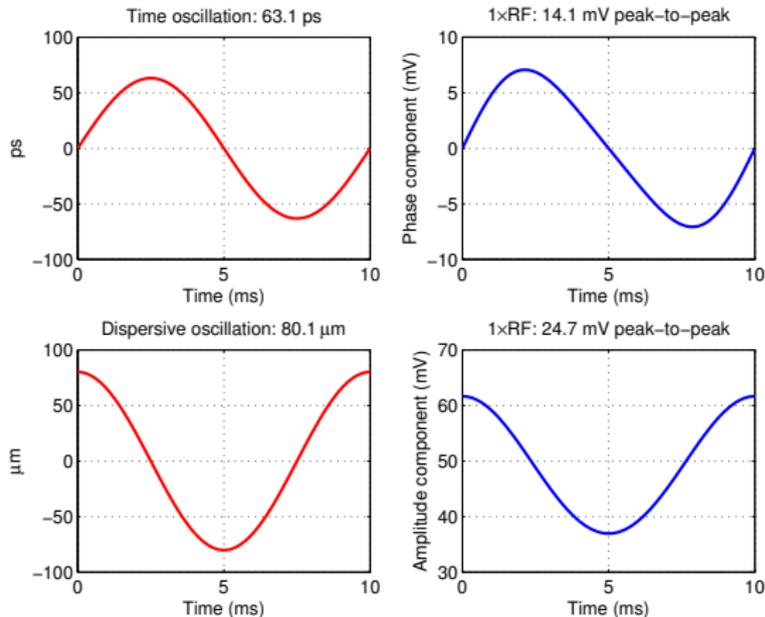
Large Orbit Offset Case



- 320 μm offset;
- 352 MHz;
- 704 MHz;
- 1056 MHz;
- 1408 MHz;
- Very high distortion.



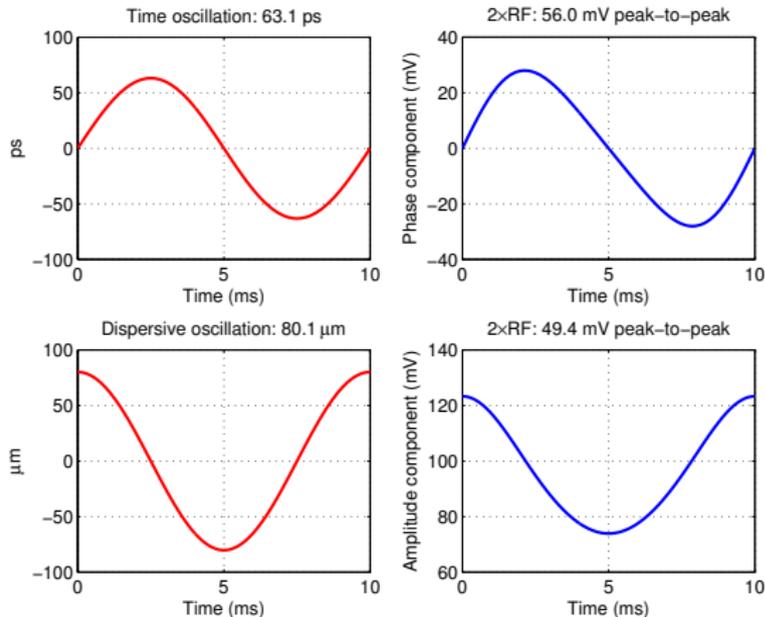
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- Very high distortion.



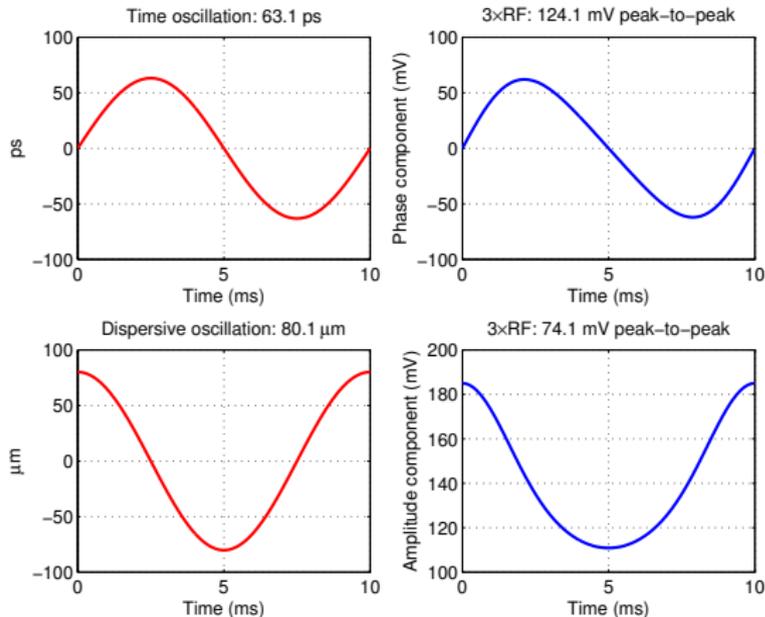
Large Orbit Offset Case



- 320 μm offset;
- 352 MHz;
- 704 MHz;
- 1056 MHz;
- 1408 MHz;
- Very high distortion.



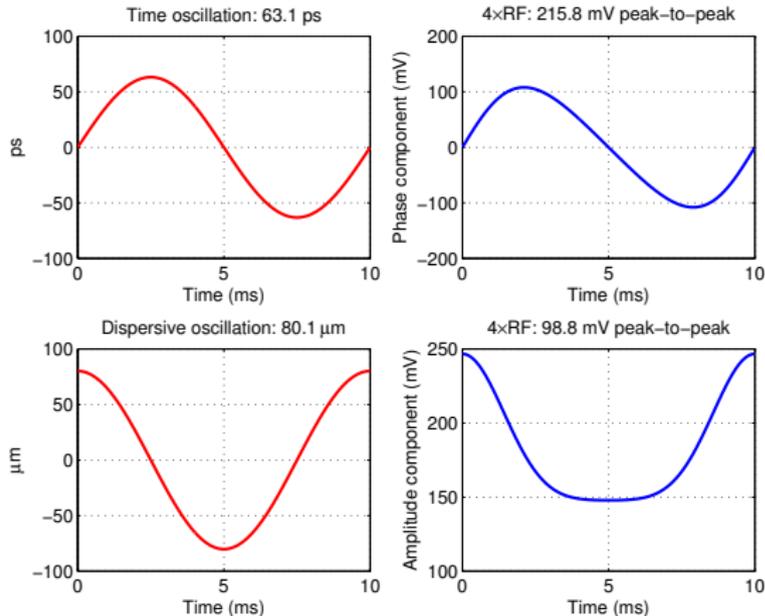
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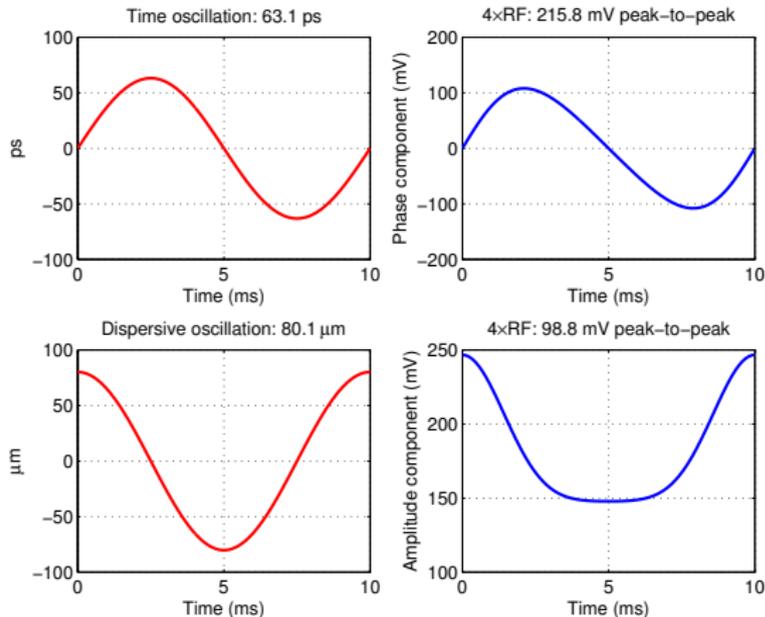
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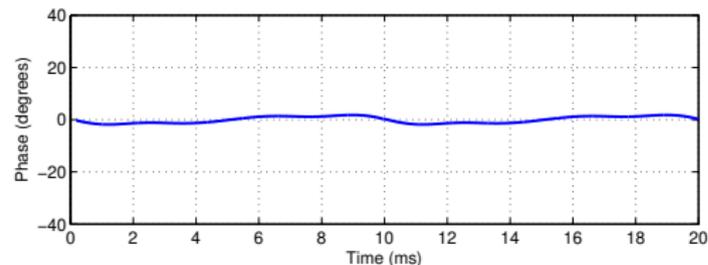
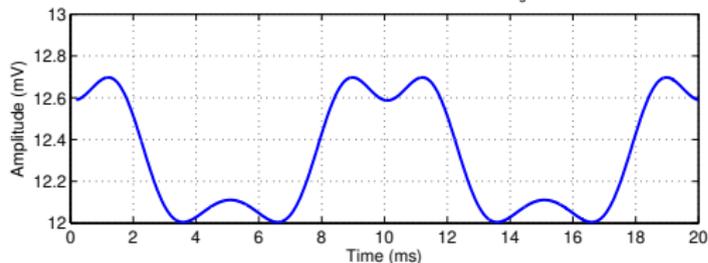


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Amplitude and Phase Relative to Synchrotron Reference, Large Offset Case

1xRF: Amplitude detector output at ω_s

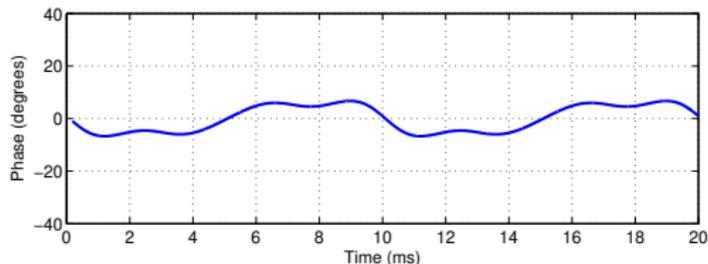
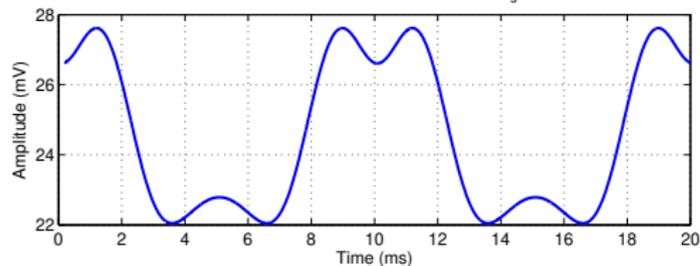


- 352 MHz;
- 704 MHz;
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- Extreme amplitude and phase modulation!



Amplitude and Phase Relative to Synchrotron Reference, Large Offset Case

2×RF: Amplitude detector output at ω_s

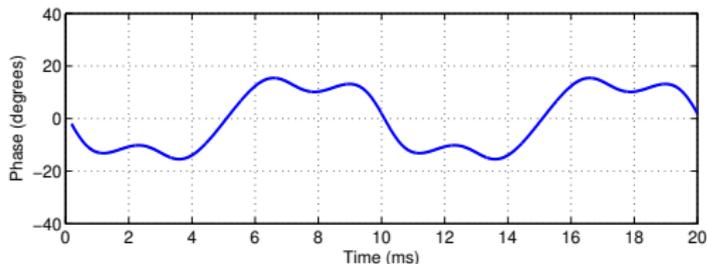
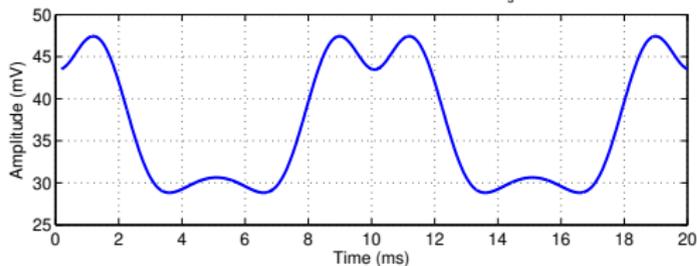


- 352 MHz;
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Amplitude and Phase Relative to Synchrotron Reference, Large Offset Case

3×RF: Amplitude detector output at ω_s

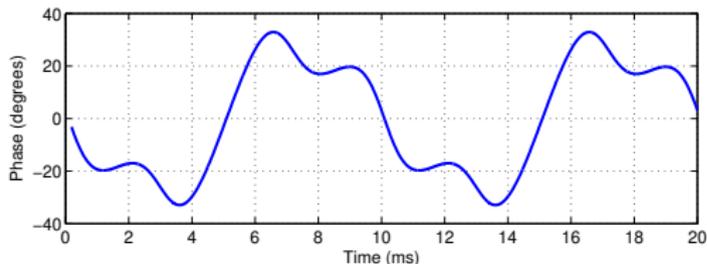
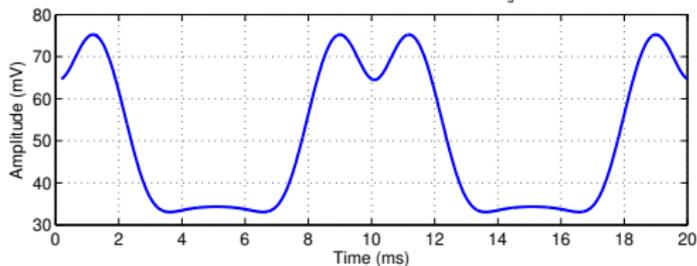


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Amplitude and Phase Relative to Synchrotron Reference, Large Offset Case

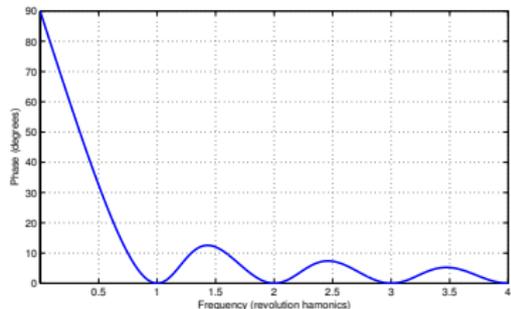
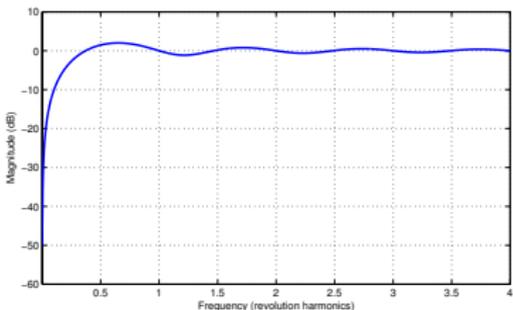
4xRF: Amplitude detector output at ω_s



- 352 MHz;
- 704 MHz;
- 1056 MHz;
- 1408 MHz;
- Extreme amplitude and phase modulation!



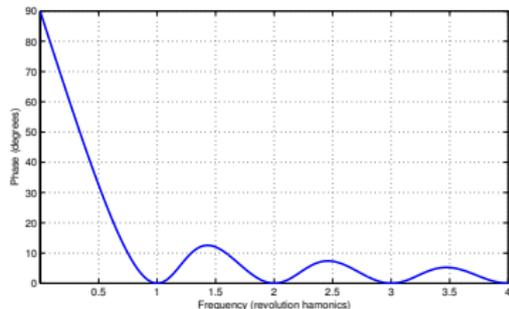
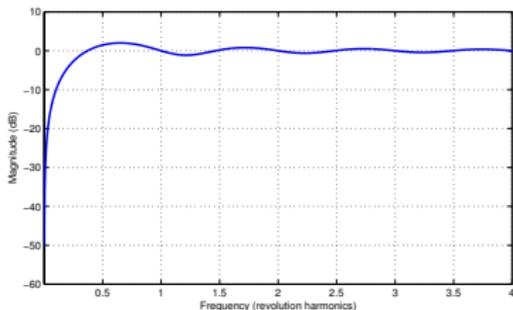
Filtering Out Mode 0



- A 1296 tap FIR filter acting on consecutive buckets;
- Signal for the turn-by-turn feedback filter is current bunch signal minus the average over the full turn;
- High rejection of low frequencies, close to unity gain by the first revolution harmonic;
- Gain is nearly perfect near revolution harmonics;
- Ripple between revolution harmonics should not be a problem;
- Efficient CIC implementation.



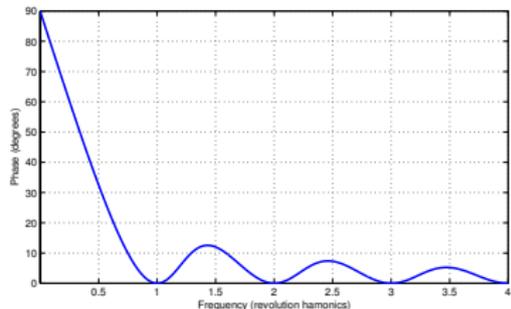
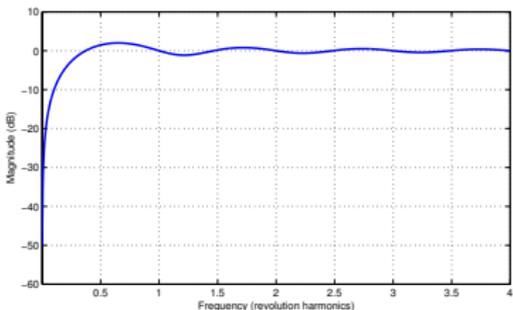
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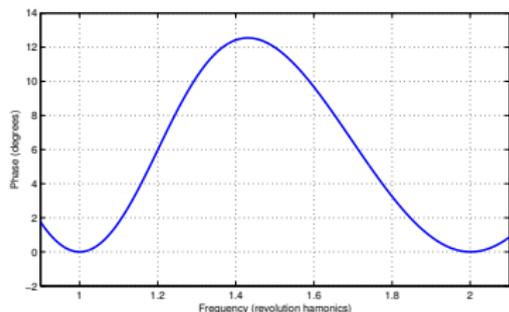
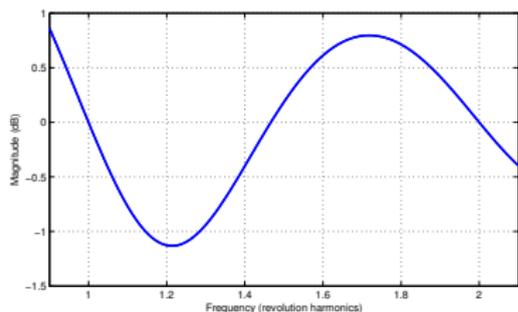
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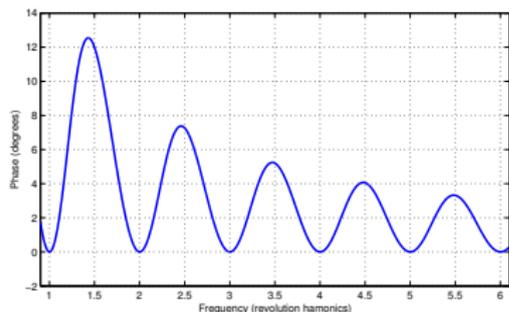
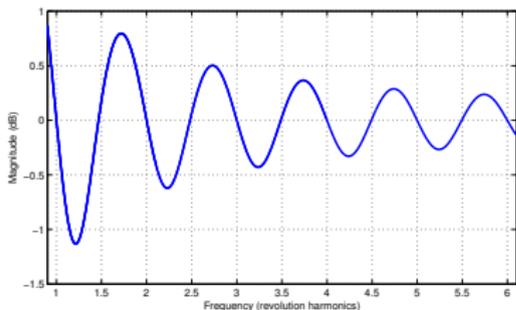
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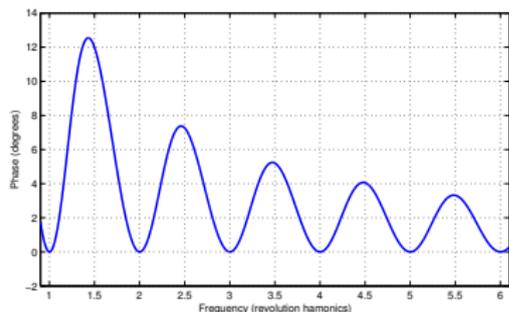
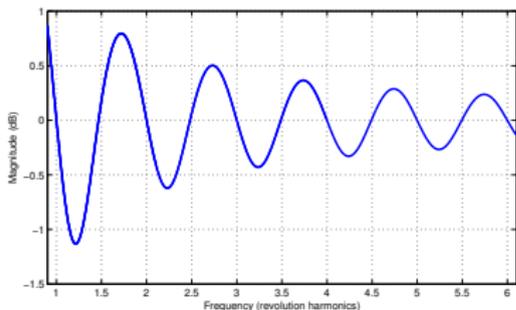
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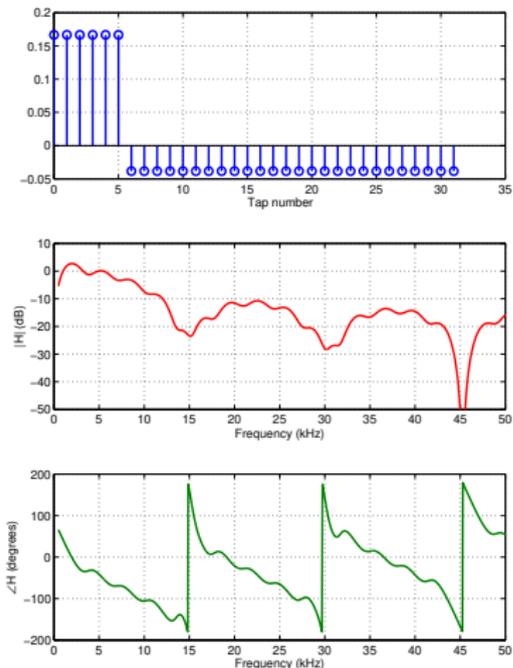
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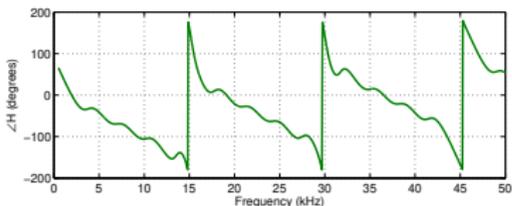
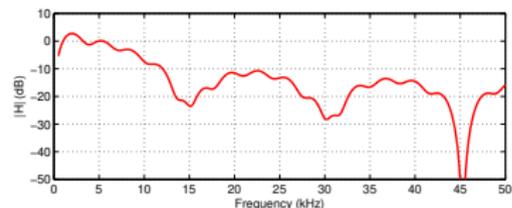
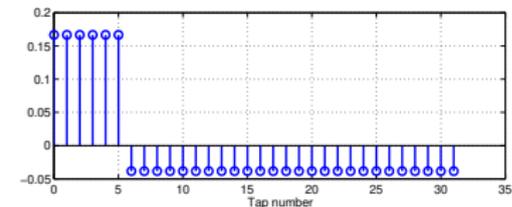
Dispersive Feedback Filter to Test in the APS



- 32-tap FIR, downsampling of 3 — can run in current iGp12 without any modifications;
- Simple-minded design - 6 tap averager to reject horizontal motion;
- Use remaining 26 taps to achieve DC rejection;
- Notch around horizontal frequency (45 kHz);
- Peak gain and nearly zero phase shift at 2.2 kHz;
- Not optimal, just a rough idea.



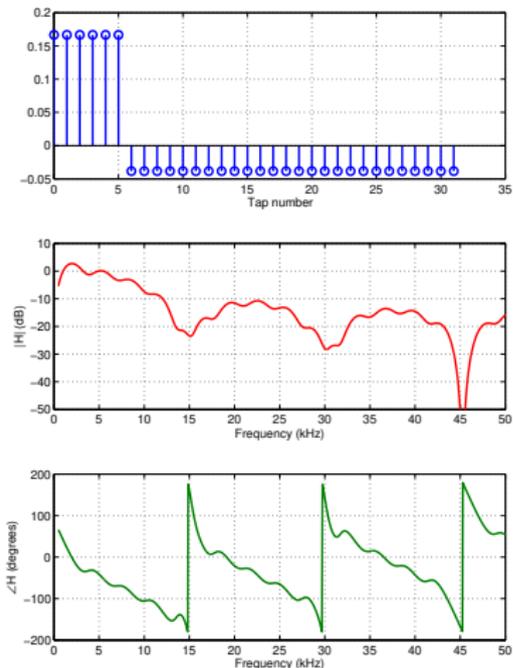
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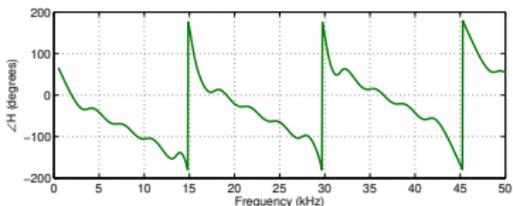
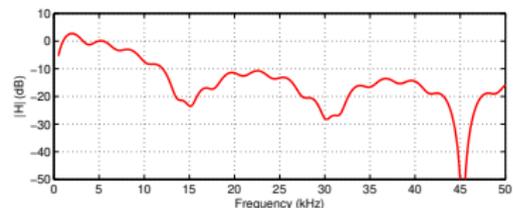
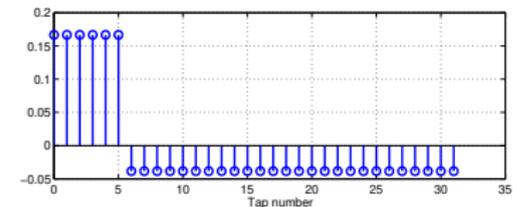
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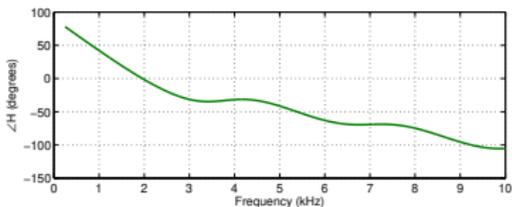
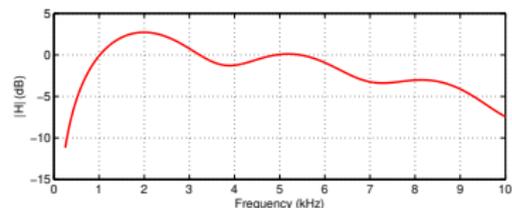
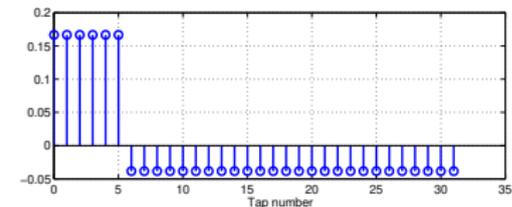
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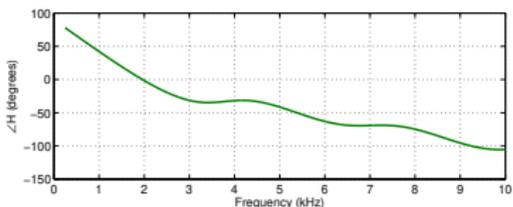
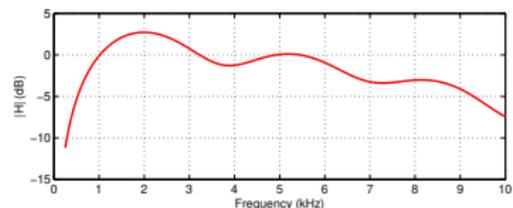
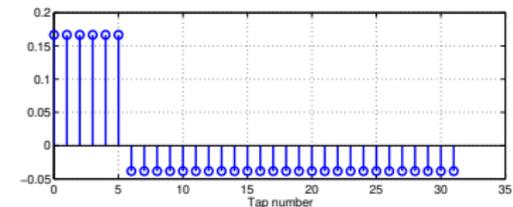
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